

## Linked List

An *array* is a very useful data structure provided in programming languages. However, it has at least two limitations:

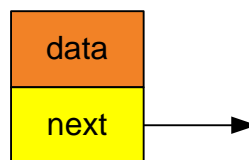
- its size has to be known at compilation time and
- the data in the array are separated in computer memory by the same distance, which means that inserting an item inside the array requires shifting other data in this array.

This limitation can be overcome by using *linked structures*. A linked structure is a collection of nodes storing data and links to other nodes. In this way, nodes can be located anywhere in memory, and passing from one node of the linked structure to another is accomplished by storing the addresses of other nodes in the linked structure. Although linked structures can be implemented in a variety of ways, the most flexible implementation is by using *pointers*.

### Singly Linked Lists

If a node contains a data member that is a pointer to another node, then many nodes can be strung together using only one variable to access the entire sequence of nodes. Such a sequence of nodes is the most frequently used implementation of a *linked list*, which is a data structure composed of nodes, each node holding some information and a pointer to another node in the list. If a node has a link only to its successor in this sequence, the list is called a *singly linked list*.

Each node in the list is an instance of the following class definition:



```
class Node
{
    int data;
    Node next;
    public Node ()
    {
        data = 0 ;
        next = null;
    }
    public Node (int data)
    {
        this.data = data;
        this.next = null;
    }
}
```

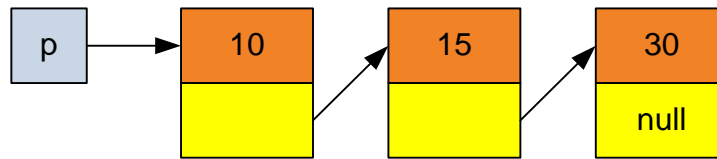
A node includes two data members: *data* and *next*. The *data* member is used to store information, and this member is important to the user. The *next* member is used to link nodes to form a linked list. It is an auxiliary data member used to maintain the linked list. It is indispensable for implementation of the linked list, but less important (if at all) from the user's perspective. Note that *Node* is defined in terms of itself because one data member, *next*, is a pointer to a node of the same type that is just being defined. Objects that include such a data member are called *self-referential objects*.

The definition of a node also includes two constructors:

- the first constructor initializes the *next* pointer to null and leaves the value of *data* unspecified.
- the second constructor takes two arguments: one to initialize the *data* member and another to initialize the *next* member. The second constructor also covers the case when

only one numerical argument is supplied by the user. In this case, *data* is initialized to the argument and *next* to **null**.

Let us create the next linked list:



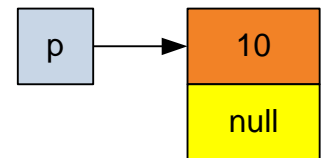
One way to create this three-node linked list is to first generate the node for number 10, then the node for 15, and finally the node for 30. Each node has to be initialized properly and incorporated into the list.

Create the first node on the list and make the variable *p* a pointer to this node:

```
Node p = new Node(10);
```

This done in four steps:

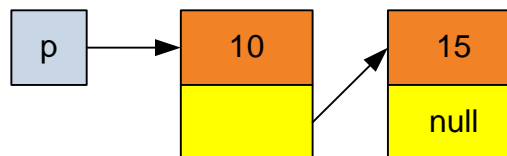
- Create a new *Node*;
- The *data* member of this node is set to 10;
- the node's *next* member is set to **null**;
- make *p* a pointer to the newly created node. This pointer is the *address* of the node, and it is shown as an arrow from the variable *p* to the new node.



The second node is created with the assignment:

```
p.next = new Node(15);
```

Here *p.next* is the *next* member of the node pointed to by *p*.



The linked list is now extended by adding a third node with the assignment

```
p.next.next = new Node(30);
```

Here *p.next.next* is the *next* member of the second node. This cumbersome notation has to be used because the list is accessible only through the variable *p*.

Our linked list example illustrates a certain inconvenience in using references: the longer the linked list, the longer the chain of *nexts* to access the nodes at the end of the list. In this example, *p.next.next.next* allows us to access the *next* member of the 3rd node on the list. But what if it were the 103<sup>rd</sup> or, worse, the 1,003<sup>rd</sup> node on the list? Typing 1,003 *nexts*, as in *p.next...next*, would be daunting. If we missed one *next* in this chain, then a wrong assignment is made. Also, the flexibility of using linked lists is diminished. Therefore, other ways of accessing nodes in linked lists are needed.

```
import java.util.*;

class Node
{
```

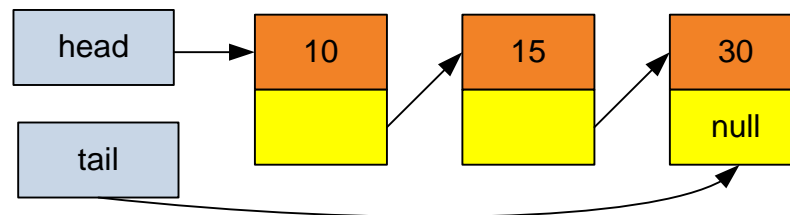
```

int data;
Node next;
public Node ()
{
    data = 0;
    next = null;
}
public Node(int data)
{
    this.data = data;
    this.next = null;
}
}

public class Main
{
    public static void main(String[] args)
    {
        Node p = new Node(10);
        p.next = new Node(15);
        p.next.next = new Node(30);
        System.out.println(p.data + " " + p.next.data + " " + p.next.next.data);
    }
}

```

One way is always to keep two pointers to the linked list: one to the first node and one to the last:



The singly linked list implementation uses two classes: one class, **Node**, for nodes of the list, and another, **LinkedList**, for access to the list. The class **LinkedList** defines two data members, *head* and *tail*, which are pointers to the first and the last nodes of a list. Method `Empty()` checks if the list is empty:

```

class LinkedList
{
    Node head, tail;
    public LinkedList ()
    {
        head = null;
        tail = null;
    }
    public boolean Empty ()
    {
        return head == null;
    }
}

```

Besides the *head* and *tail* members, the class **LinkedList** also defines member functions that allow us to manipulate the lists. We now look more closely at some basic operations on linked lists.

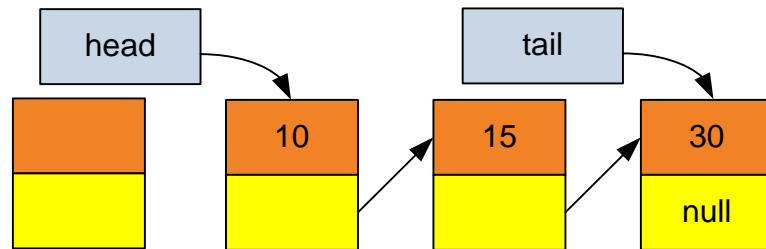
The list is declared with the statement:

```
LinkedList list = new LinkedList();
```

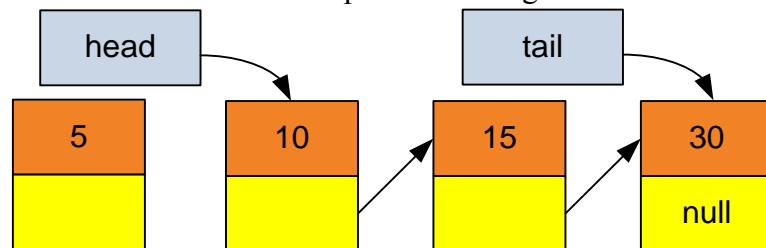
## Insertion

Adding a node at the *beginning* of a linked list is performed in four steps:

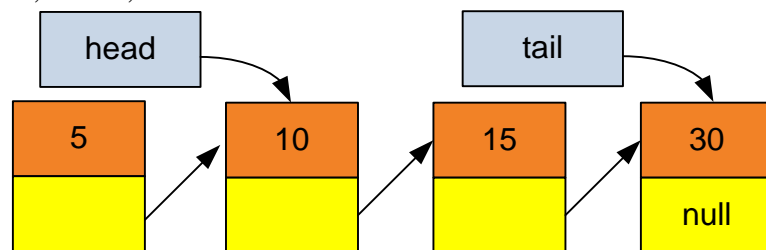
1. An *empty* node is created. It is empty in the sense that the program performing insertion does not assign any values to the data members of the node.



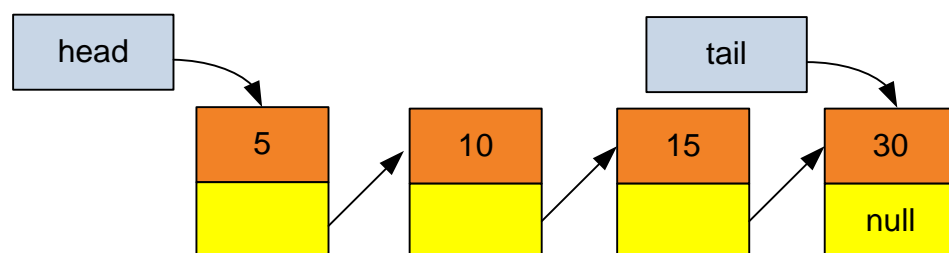
2. The node's info member is initialized to a particular integer.



3. Because the node is being included at the front of the list, the *next* member becomes a pointer to the first node on the list; that is, the current value of *head*.



4. The new node precedes all the nodes on the list, but this fact has to be reflected in the value of *head*; otherwise, the new node is not accessible. Therefore, *head* is updated to become the pointer to the new node.



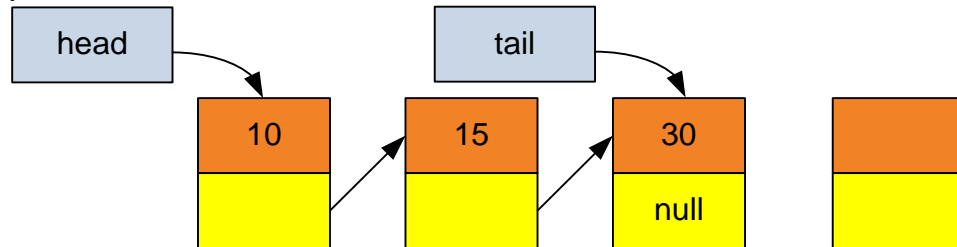
The four steps are executed by the member function `addToHead()`:

```
public void addToHead(int val)
{
    if (tail == null) // list is empty
        head = tail = new Node(val);
    else
    {
        Node temp = new Node(val);
        temp.next = head;
        head = temp;
    }
}
```

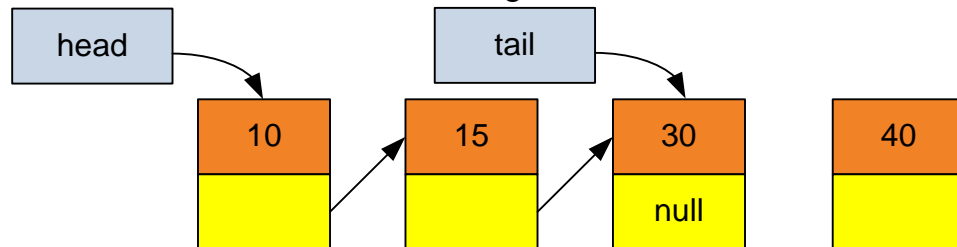
The member function *addFirst* () singles out one special case, namely, inserting a new node in an empty linked list. In an empty linked list, both *head* and *tail* are null; therefore, both become references to the only node of the new list. When inserting in a nonempty list, only *head* needs to be updated.

The process of adding a new node *to the end* of the list has five steps.

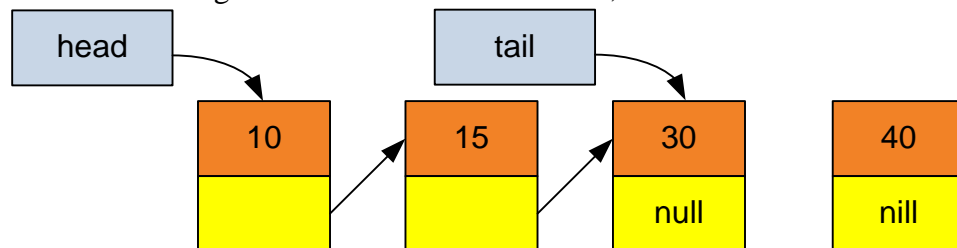
1. An empty node is created.



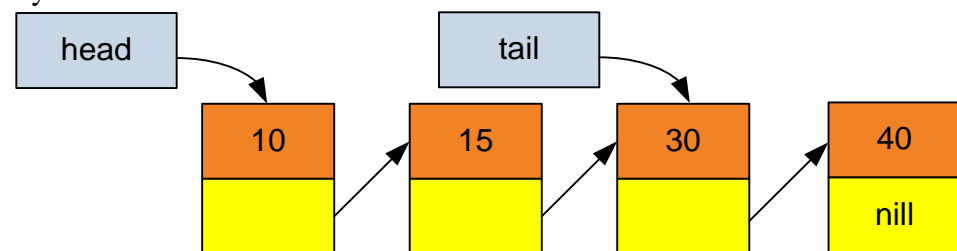
2. The *node*'s info member is initialized to an integer *val*.



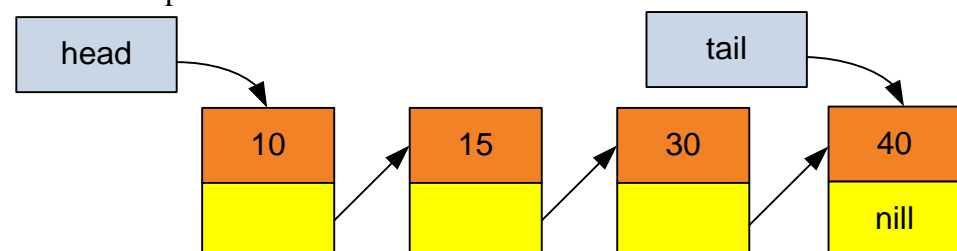
3. Because the node is being included at the end of the list, the *next* member is set to null.



4. The node is now included in the list by making the *next* member of the last node of the list a pointer to the newly created node.



5. The new node follows all the nodes of the list, but this fact has to be reflected in the value of *tail*, which now becomes the pointer to the new node.



```

public void addLast(int val)
{
    if (tail != null) // list is not empty
    {
        tail.next = new Node(val);
        tail = tail.next;
    }
    else head = tail = new Node(val);
}

```

All these steps are executed in the if clause of *addLast()*. The else clause of this function is executed only if the linked list is empty. If this case were not included, the program may crash because in the if clause we make an assignment to the *next* member of the node referred by *tail*. In the case of an empty linked list, it is a pointer to a nonexisting data member of a nonexisting node.

## Deletion

First we consider deletion a node from the *beginning* of the list. Function returns *true* if deletion is successful, otherwise *false*. There are now two special cases to consider:

- One case is when we attempt to remove a node from an empty linked list. If such an attempt is made, the program is very likely to crash, which we don't want to happen. So in this case we do nothing, but simply return *false*.
- The second special case is when the list has only one node to be removed. In this case, the list becomes empty, which requires setting *tail* and *head* to *null*.

```

public boolean removeFirst()
{
    if (Empty()) return false;
    if (head == tail) // only one node in a list
        head = tail = null;
    else head = head.next;
    return true;
}

```

Now consider the process of deleting a node from the end of the list. It is implemented as the member function *removeLast()*. The problem is that after removing a node, *tail* should refer to the new tail of the list; that is, *tail* has to be moved backward by one node. But moving backward is impossible because there is no direct link from the last node to its predecessor. Hence, this predecessor has to be found by searching from the beginning of the list and stopping right before *tail*. This is accomplished with a temporary variable *temp* that scans the list within the **for** loop. The variable *temp* is initialized to the *head* of the list, and then in each iteration of the loop it is advanced to the next node.

In removing the last node, the two special cases are the same as in *removeFirst()*:

- If the list is empty, then nothing can be removed;
- When a single-node list becomes empty after removing its only node, which also requires setting *head* and *tail* to *null*.

```

public boolean removeLast()
{
    if (Empty()) return false;
    if (head == tail) // only one node in a list
    {
        head = tail = null;
    }
    else // if more than one node in the list
    {
        Node temp;
        // find the predecessor of tail

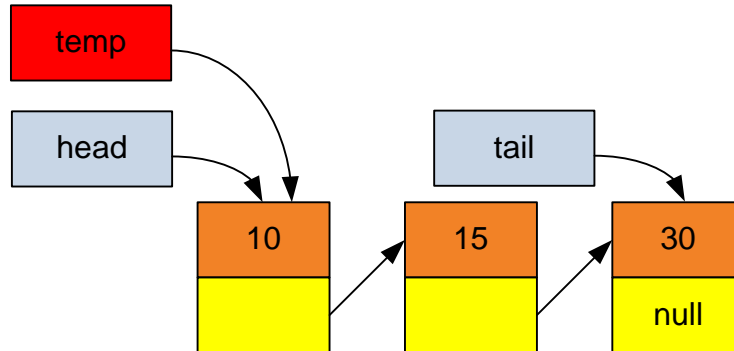
```

```

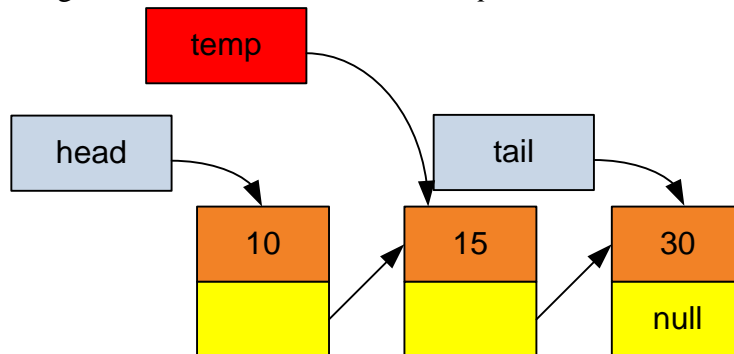
    for(temp = head; temp.next != tail; temp = temp.next);
    tail = temp; // the predecessor of tail becomes tail
    tail.next = null;
}
return true;
}

```

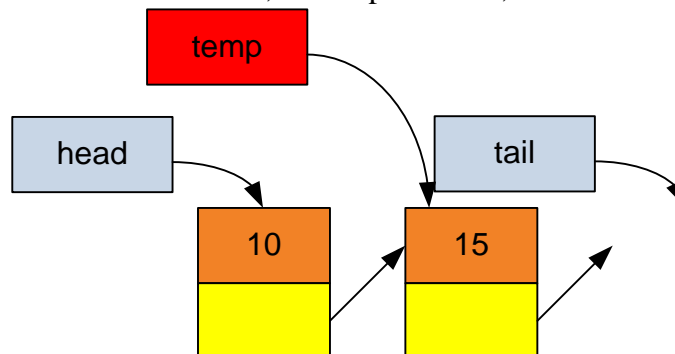
Consider the list, where *temp* first refers to the head node holding number 10:



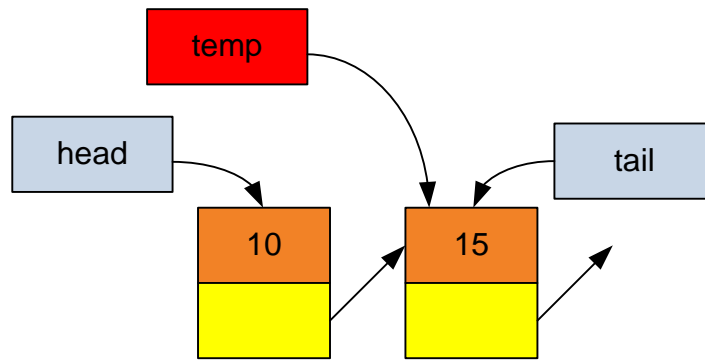
After executing the assignment `temp = temp.next`, *temp* refers to the second node:



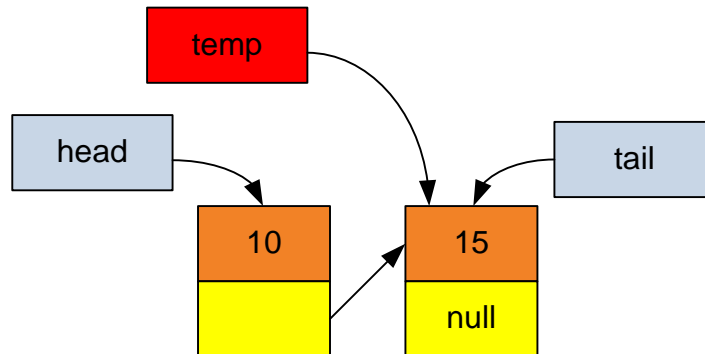
Because this node is the next to last node, the loop is exited, after which the last node is deleted:



Because *tail* is now pointing to a nonexistent node, it is immediately set to point to the next to last node currently pointed to by *temp*:



To mark the fact that it is the last node of the list, the *next* member of this node is set to **null**:



The most time-consuming part of `deleteFromTail()` is finding the next to last node performed by the for loop. It is clear that the loop performs  $n - 1$  iterations in a list of  $n$  nodes, which is the main reason this member function takes  $O(n)$  time to delete the last node.

### Java implementation:

```
import java.util.*;

class ListNode
{
    int data;
    ListNode next;
    public ListNode(int data)
    {
        this.data = data;
        this.next = null;
    }
}

class LinkedList
{
    ListNode head, tail;
    public LinkedList()
    {
        head = null;
        tail = null;
    }

    public boolean Empty()
    {
        return head == null;
    }
}
```



```

public void addFirst(int val)
{
    if (tail == null) // list is empty
        head = tail = new ListNode(val);
    else
    {
        ListNode temp = new ListNode(val);
        temp.next = head;
        head = temp;
    }
}

public void addLast(int val)
{
    if (tail != null) // list is not empty
    {
        tail.next = new ListNode(val);
        tail = tail.next;
    }
    else head = tail = new ListNode(val);
}

public boolean removeFirst()
{
    if (Empty()) return false;
    if (head == tail) // only one node in a list
        head = tail = null;
    else head = head.next;
    return true;
}

public boolean removeLast()
{
    if (Empty()) return false;
    if (head == tail) // only one node in a list
    {
        head = tail = null;
    }
    else // if more than one node in the list
    {
        ListNode temp;
        // find the predecessor of tail
        for(temp = head; temp.next != tail; temp = temp.next);
        tail = temp; // the predecessor of tail becomes tail
        tail.next = null;
    }
    return true;
}

public void Print()
{
    ListNode head = this.head;
    while(head != null)
    {
        System.out.print(head.data + " ");
        head = head.next;
    }
}

```

```

        System.out.println();
    }
}

public class Main
{
    public static void main(String[] args)
    {
        LinkedList list = new LinkedList();
        list.addFirst(10);    list.addFirst(15);
        list.removeLast();   list.addFirst(20); // 20 15
        list.Print();

        list.addLast(30);    list.addLast(35);
        list.addFirst(77);   list.addFirst(99); // 99 77 20 15 30 35
        list.Print();

        list.removeFirst(); list.removeFirst();
        list.removeFirst(); list.removeLast(); // 15 30
        list.Print();
    }
}

```

### **C++ implementation:**

```

#include <stdio.h>

class ListNode
{
public:
    int data;
    ListNode *next;
    ListNode(int data) : data(data), next(NULL) {}
};

class LinkedList
{
public:
    ListNode *head, *tail;
    LinkedList()
    {
        head = NULL;
        tail = NULL;
    }

    bool Empty()
    {
        return head == NULL;
    }

    void addFirst(int val)
    {
        if (tail == NULL) // list is empty
            head = tail = new ListNode(val);
        else
        {
            ListNode *temp = new ListNode(val);
            temp->next = head;
        }
    }
}

```

```

        head = temp;
    }
}

void addLast(int val)
{
    if (tail != NULL) // list is not empty
    {
        tail->next = new ListNode(val);
        tail = tail->next;
    }
    else head = tail = new ListNode(val);
}

bool removeFirst()
{
    if (Empty()) return false;
    if (head == tail) // only one node in a list
        head = tail = NULL;
    else head = head->next;
    return true;
}

bool removeLast()
{
    if (Empty()) return false;
    if (head == tail) // only one node in a list
    {
        head = tail = NULL;
    }
    else // if more than one node in the list
    {
        ListNode *temp;
        // find the predecessor of tail
        for (temp = head; temp->next != tail; temp = temp->next);
        tail = temp; // the predecessor of tail becomes tail
        tail->next = NULL;
    }
    return true;
}

void Print()
{
    ListNode *head = this->head;
    while (head != NULL)
    {
        printf("%d ", head->data);
        head = head->next;
    }
    printf("\n");
}

int size()
{
    int cnt = 0;
    ListNode *head = this->head;
    while (head != NULL)
    {

```

```
        cnt++;
        head = head->next;
    }
    return cnt;
}
};

int i, n, x, cyc;
ListNode *temp;

int main(void)
{
    scanf("%d", &n);
    LinkedList *list = new LinkedList();
    if (list->Empty()) printf("Empty\n");
    list->addFirst(10); list->addFirst(13);
    list->addLast(20); list->addLast(24);

    list->removeFirst(); list->removeLast();

    list->Print();
    printf("%d\n", list->size());

    return 0;
}
```