## 7714. Milling machines

A Fab Lab is a small open workshop where you can create or manufacture almost anything you want, mainly using computer-controlled tools such as a laser cutter or a 3D printer. Recently, the FAU Fab Lab acquired a CNC milling machine. With this machine, you can cut or remove material from the surface of a workpiece using various tools. The entire process is controlled by a computer program.

Sometimes I wondered what would happen if several workpieces of different shapes were processed using the same milling program. To simplify the situation, let’s assume that we only have two-dimensional workpieces without holes. A milling program consists of several steps, each describing which parts of the surface the milling machine should remove material from (using different tools).

**Input.** The first line contains  two integers *w* and *s* (1 ≤ *w*, *s* ≤ 104) – the number of workpieces and the number of steps in the milling program.

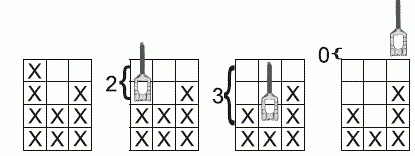
The next line contains two integers *x* and *y* (1 ≤ *x*, *y* ≤ 100), where *x* is the width of a workpiece, and *y* is its maximum possible height.

Each of the following *w* lines describes one workpiece. The description of each workpiece consists of *x* non-negative integers defining the surface height in each column.

Then follow *s* lines describing the milling steps. Each milling step consists of *x* non-negative integers *si* (0 ≤ *si* ≤ *y*), determining how much material should be removed in each column (relative to the milling area height, i.e., relative to *y*, not to the top of the workpiece). See the illustration.

**Output.** For each workpiece, print one line containing  integers – the remaining surface heights after all milling steps (in the same order as in the input).

**Figure.** In the first example, you can see how the second workpiece looks after applying all milling steps sequentially: each value in the program defines the vertical position of the milling head.



|  |  |
| --- | --- |
| **Sample input 1** | **Sample output 1** |
| 2 1  3 4  4 4 4  4 2 3  2 3 0 | 2 1 4  2 1 3 |
|  |  |
| **Sample input 2** | **Sample output 2** |
| 1 3  10 100  11 22 33 44 55 66 77 88 99 100  1 100 1 100 1 100 1 100 1 100  58 58 58 58 58 58 58 58 58 58  42 42 42 42 42 42 42 42 66 42 | 11 0 33 0 42 0 42 0 34 0 |

## SOLUTION

**mathematics**

**Algorithm analysis**

The milling program consists of *s* steps. Let at the -th step () a layer of thickness *mij* be removed from the surface in column *j* (1 ≤ *j* ≤ *x*). It is clear that the total amount removed in column *j* will be

max(*m*1*j*, *m*2*j*, …, *m*s*j*)

We’ll call the milling scheme the set of integers

(*cuts*1, *cuts*2, …, *cutsx*),

where

*cutsj* = max(*m*1*j*, *m*2*j*, …, *m*s*j*), 1 ≤ *j* ≤ *x*



The same milling scheme is applied to all *w* workpieces. After computing the values of *cutsj* (1 ≤ *j* ≤ *x*), this scheme is then applied sequentially to each workpiece.

**Algorithm implementation**

Declare the arrays. The information about the workpieces is stored in the array *detail*, and the milling scheme is stored in the array *cuts*.

int detail[10001][101], cuts[101];

Read the input data.

scanf("%d %d %d %d", &w, &s, &x, &y);

Read the information about the *w* workpieces.

for (i = 0; i < w; i++)

for (j = 0; j < x; j++)

scanf("%d", &detail[i][j]);

Read and process the *s* steps of the milling program. For each position *j*, the value cuts[*j*] represents the maximum cutting depth achieved at any of the steps.

for (i = 0; i < s; i++)

for (j = 0; j < x; j++)

{

scanf("%d", &val);

if (val > cuts[j]) cuts[j] = val;

}

The maximum possible height of a workpiece is *y*. The milling head at position *j* is lowered to a depth of cuts[*j*]. Consequently, after milling, the remaining height of the *i*-th workpiece at position *j* will be equal to

min(detail[*i*][*j*], *y* – cuts[*j*]).

for (i = 0; i < w; i++)

{

for (j = 0; j < x; j++)

printf("%d ", min(detail[i][j], y - cuts[j]));

printf("\n");

}